

# Model Documentation of the Buck Converter

## 1 Nomenclature

### 1.1 Nomenclature for Model Equations

|       |                              |
|-------|------------------------------|
| $L$   | inductivity of the inductor  |
| $C$   | capacity of the capacitor    |
| $R$   | resistance of the load       |
| $U_E$ | input voltage                |
| $i_L$ | current through the inductor |
| $u_C$ | voltage over the capacitor   |
| $d$   | duty ratio of the switch     |

### 1.2 Circuit Diagram

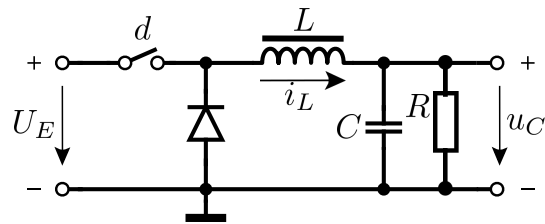


Figure 1: Circuit

## 2 Model Equations

State Vector and Input Vector:

$$\underline{x} = (x_1 \ x_2)^T = (i_L \ u_C)^T$$
$$\underline{u} = d$$

System Equations:

$$\dot{x}_1 = -\frac{1}{L}x_2 + \frac{U_E}{L}u \quad (1a)$$

$$\dot{x}_2 = \frac{1}{C}x_1 - \frac{1}{RC}x_2 \quad (1b)$$

Parameters:  $L, C, R, U_E$

Outputs:  $x_2 = u_C$

## 2.1 Exemplary parameter values

|               | Symbol | Value               |          |
|---------------|--------|---------------------|----------|
| Inductivity   | $L$    | 0.00018             | H        |
| Capacity      | $C$    | $2.0 \cdot 10^{-5}$ | F        |
| Resistance    | $R$    | 10                  | $\Omega$ |
| Input Voltage | $U_E$  | 24                  | V        |

## 3 Derivation and Explanation

See boost converter.

## 4 Simulation

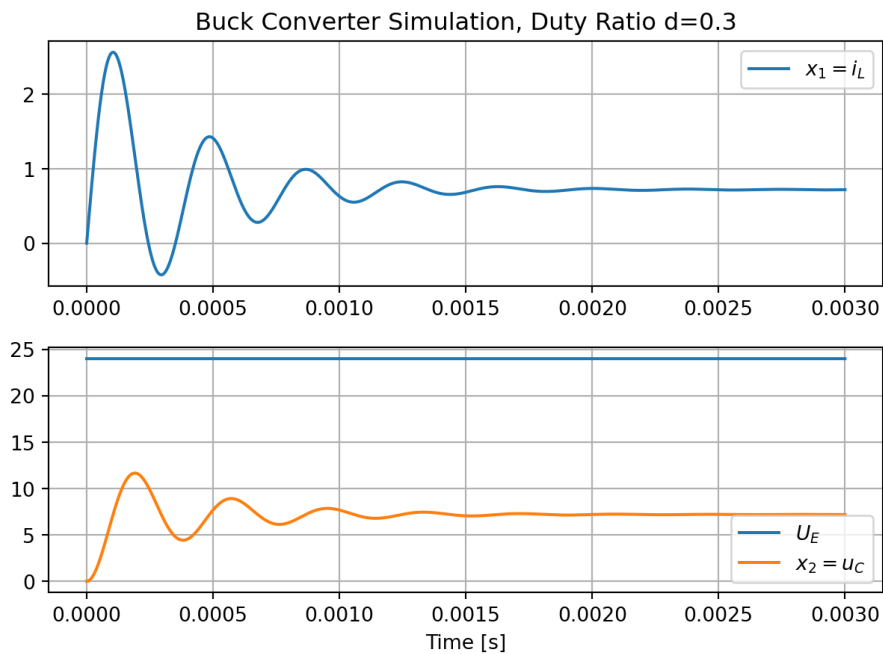


Figure 2: Simulation of the buck converter.

## References

- [1] R. H. G. Tan and L. Y. H. Hoo, DC-DC converter modeling and simulation using state space approach, in 2015 IEEE Conference on Energy Conversion (CENCON), Oct. 2015, pp. 42–47. doi: 10.1109/CENCON.2015.7409511.
- [2] K. Röbenack, Nichtlineare Regelungssysteme: Theorie und Anwendung der exakten Linearisierung. Berlin, Heidelberg: Springer Berlin Heidelberg, 2017. doi: 10.1007/978-3-662-44091-9.