

# Model Documentation of the 'Inverted pendulum'

## 1 Nomenclature

### 1.1 Nomenclature for Model Equations

- $x$  state vector
- $u$  control input vector
- $w$  noise vector
- $z$  regulated output vector
- $y$  measurement vector

## 2 Model Equations

State Vector and Input Vector:

$$x \in \mathbb{R}^6 \quad u \in \mathbb{R}^2 \quad w \in \mathbb{R}^2 \quad z \in \mathbb{R}^2 \quad y \in \mathbb{R}^4$$

System Equations:

$$\dot{x}(t) = Ax(t) + B_1w(t) + Bu(t) \tag{1a}$$

$$z(t) = C_1x(t) + D_{11}w(t) + D_{12}u(t) \tag{1b}$$

$$y(t) = Cx(t) + D_{21}w(t) \tag{1c}$$

Outputs:  $z$

## 2.1 Exemplary parameter values

Symbol	Value
$A$	$\begin{bmatrix} 0 & 1.0 & 0 & 0 & 0 & 0 \\ 48.9844 & 0 & -48.9844 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.18494 & 0 & 0 \\ 0 & 0 & 0 & -50.0 & 0 & 0 \\ 0 & 0 & -0.5 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$
$B$	$\begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 50.0 \\ 0 & 0 \\ 0 & 0 \\ 1.0 & 0 \end{bmatrix}$
$B_1$	$\begin{bmatrix} 0 & 0 \\ 0 & 50.0 \\ 0 & 0 \\ 0 & 0 \\ 1.0 & 0 \end{bmatrix}$
$C_1$	$\begin{bmatrix} 0 & 0 & 0 & 0.0036988 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1.0 & 0 \end{bmatrix}$
$C$	$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 1.0 \\ 0 & 0 & 1.0 & 0 & 0 & 0 \\ 1.0 & 0 & -1.0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1.0 & 0 \end{bmatrix}$
$D_{11}$	$\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$
$D_{12}$	$\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$
$D_{21}$	$\begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$

## 3 Derivation and Explanation

This model is part of the "COMpleib" - library and was automatically imported into ACKREP.

The original description was:

ROC10 Inverted pendulum P. Apkarian and H. D. Tuan, "Robust Control via Concave Minimization, Local and Global Algorithms", TOAC, Vol. 45, Nr. 2, pp. 299-305, 2000 Ex. 1

## 4 Simulation

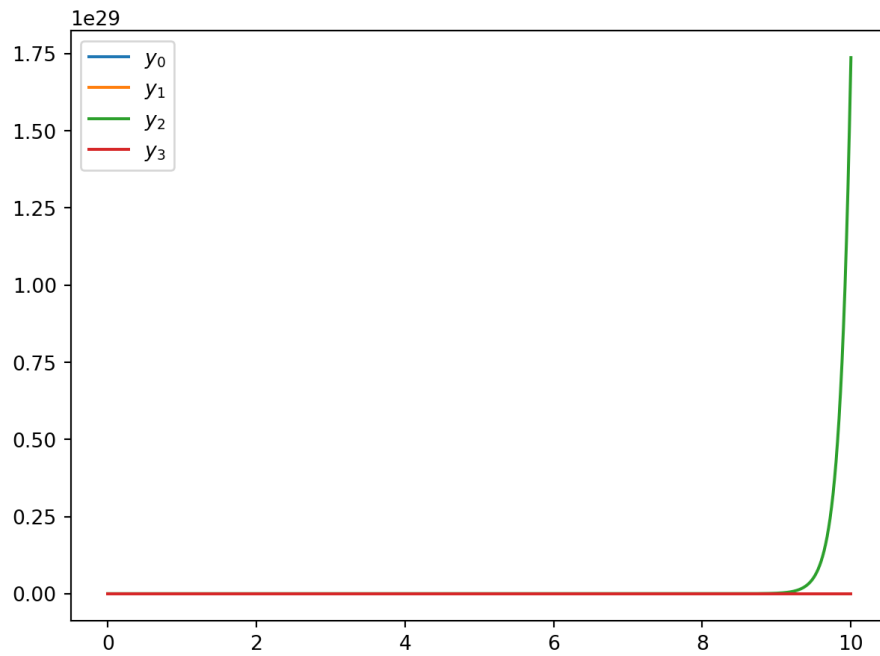


Figure 1: Simulation of the Inverted pendulum.

## References

- [1] . Apkarian and H. D. Tuan, "Robust Control via Concave Minimization, Local and Global Algorithms", TOAC, Vol. 45, Nr. 2, pp. 299-305, 2000  
Ex. 1